

# PAPR REDUCTION OF OFDM SIGNALS USING MULTIPLE SYMBOL REPRESENTATIONS – CLIPPING HYBRID SCHEME

Victor Cuteanu, Alexandru Isar, Corina Nafornta

Communications Department, Electronics and Telecommunications Faculty, Politehnica University, Timisoara, Romania  
victor.cuteanu@gmail.com, alexandru.isar@etc.upt.ro, corina.nafornta@etc.upt.ro

## ABSTRACT

*This paper presents a new hybrid PAPR reduction technique for the OFDM signal, which combines a multiple symbol representations method with a signal clipping method. The simulation results highlight the advantages of the proposed PAPR reduction method.*

**Keywords:** OFDM, PAPR, multiple symbol representation, clipping.

## 1. INTRODUCTION

The Orthogonal Frequency Division-Multiplexing (OFDM) is one of the most popular technologies used in broadband wireless communication systems like WiMAX, DVB-T or ADSL. One of the main practical issues of the OFDM is the Peak-to-Average Power Ratio (PAPR) of the transmitted signal. Large signal peaks requires the power amplifiers (PA) to support wide linear dynamic range. Higher signal level causes non-linear distortions leading to an inefficient operation of PA causing intermodulation products resulting unwanted out-of-band power. In order to reduce the PAPR of OFDM signals, many solutions have been proposed and analyzed. The efficiency of these methods can be evaluated considering their characteristics of non-linearity, amount of processing and size of side information needed to be sent to receiver.

The clipping method is a nonlinear PAPR reduction scheme, where the amplitude of the signal is limited to a given threshold. Considering the fact that the signal must be interpolated before A/D conversion, a variety of clipping methods has been proposed.

Some methods suggest the clipping before interpolation, having the disadvantage of the peaks regrowth. Other methods suggest the clipping after interpolation, having the disadvantage of out-of-band power production. In order to overcome this problem different filtering techniques have been proposed. Filtering can also cause peak regrowth, but less than the clipping before interpolation [1].

Another clipping technique supposes that only subcarriers having the highest phase difference between the original signal and its clipped variant will be changed. This is the case of the partial clipping (PC) method [10].

To further reduce the PAPR, the dynamic of the clipped signal can be compressed. Some papers proposed  $\mu$ -law/A-law companding functions [11], [8], exponential companding function [13] or piecewise-scales [2] after the clipping.

Linear methods like partial transmit sequence (PTS) or selective mapping (SLM) has been proposed for the reduction of PAPR as well. These methods generate different versions of the OFDM signal, by rotating each vector from the original signal with phases selected from a given set. Then the signal variant with the smaller PAPR is chosen for the transmission [3], [4].

Another PAPR reduction method is the tone reservation (TR). It uses tones on which no data is sent to reduce the transmitted signal peaks. Derivates of this method with lower computation complexity and improved performance have been proposed: One-Tone One-Peak (OTOP) [12] and one by-one iteration [9].

A similar PAPR reduction method is the multiple symbol representations, where alternative signalling points are used to represent one symbol. The variant proposed in [6] uses an expanded constellation comprised of the original conventional constellation and the alternative signalling points located on a circle located in the origin. The increased radius is chosen to maintain the minimum distance of the original constellation.

In the next paragraph we describe the OFDM signal structure. Next, we present the new hybrid PAPR reduction scheme where multiple symbol representations and signal clipping methods are described.

Finally, based on numerical results provided by the simulations, we analyze the performance of the new technique.

## 2. THE OFDM SIGNAL

In OFDM, the message bits are grouped in blocks  $\{X_n, n=0,1,\dots,N-1\}$ , and modulates in amplitude a set of  $N$  subcarriers,  $\{f_n, n=0,1,\dots,N-1\}$ . These subcarriers are chosen to be orthogonal, that is  $f_n=n\Delta f$ , where  $\Delta f=1/T$ , and  $T$  is the OFDM symbol period. The resulting signal can be written as:

$$x(t) = \frac{1}{\sqrt{N}} \sum_{n=0}^{N-1} X_n e^{j2\pi f_n t} \quad (1)$$

In order to avoid the intersymbol interference (ISI) generated by the multipath channels, a Cyclic Prefix (CP-corresponding to a guard interval) is added to the signal. After Digital-to-Analogue (D/A) conversion, the signal's spectrum is centred on a high frequency carrier and applied to a PA which drives the antenna load.

At the receiver, after demodulation, the CP will be removed, the symbols being evaluated for a time interval of  $[0, T]$ .

The expression of the PAPR for a given OFDM symbol is given by:

$$PAPR(x) = \frac{\max(|x(t)|^2)}{E[|x(t)|^2]}, \quad (2)$$

where  $E[\cdot]$  denotes the expectation operator.

Another quality measure refers to the non-linearity of the transmitted signal which is produced by the PA. This is the Signal-to-Distortion Ratio (SDR) defined as:

$$SDR = \frac{\|x\|^2}{\|x - g(x)\|^2} \quad (3)$$

where  $g(\cdot)$  is the memoryless nonlinearity representing the effects of the PA.

The optimal solution for PAPR problem may not be the best solution for the SDR problem and vice versa. Because these two problems are correlated, in practice a suboptimal solution may be chosen [7].

### 3. HYBRID PAPR REDUCTION METHOD

In this paragraph we present the proposed hybrid PAPR reduction technique which has been obtained by serialization of sequential tone reservation method and the signal clipping method.

The performance of the proposed PAPR reduction technique is analyzed with a MATLAB simulator as presented in Fig. 1. Within this simulator, the samples from the generated signal are grouped in blocks of same size like the OFDM symbols. Each sample, group of M bits, is transformed using the M-QAM or the M-PSK modulation, obtaining the frequency domain OFDM symbols. They are applied to the multiple symbol representations block, where the amplitude and phase of some of the data carriers are modified for the first peak reduction.

The used multiple symbol representations technique is derived from [6], and is presented in the block diagram from Fig. 2. It selects  $Q$  carrier positions from the complete set of  $N$  carriers representing the OFDM symbol. For these carriers, an extended constellation with  $R$  possible points for each symbol is considered. The obtained search space of  $R^Q$  combinations is used by the algorithm to generate alternative OFDM symbols, the one with minimum PAPR being chosen for the transmission.

This search space may lead to an increased amount of data computation. The proposed multiple symbol representations algorithm decreases the computation complexity by attempting a reduced search space by trying all  $R$  alternatives on the first carrier position  $P[0]$ , while the other carriers,  $P[1], \dots, P[Q-1]$ , have the initial state. Once an optimal value  $C[0]$  is found, a similar procedure is repeated on the other pilot positions.

The proposed multiple symbol representations algorithm considers both symmetrical and asymmetrical repartition of

data carriers selectable for PAPR reduction, as depicted in Fig. 4 and Fig. 5. The alternative symbol's points from the expanded constellation are placed on different concentric circles with the radius delta equal with the minimum distance of original constellation as presented in Fig. 3.

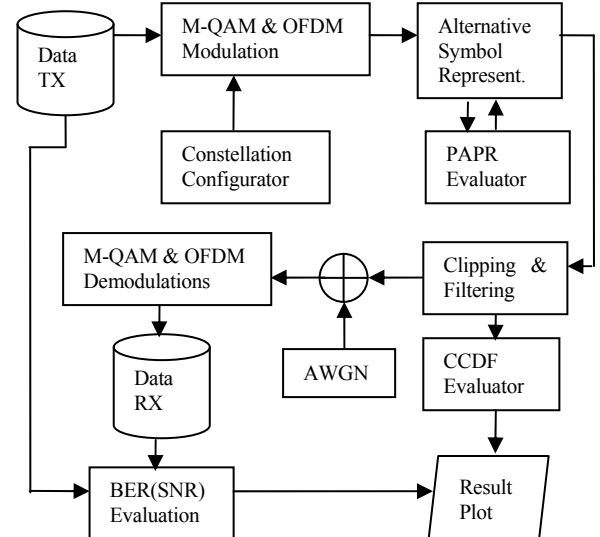


Figure 1. MATLAB model of the hybrid PAPR reduction technique.

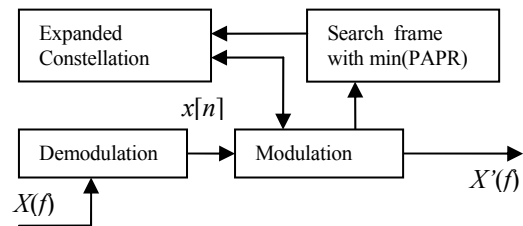


Figure 2. Multiple symbol representations PAPR reduction method.

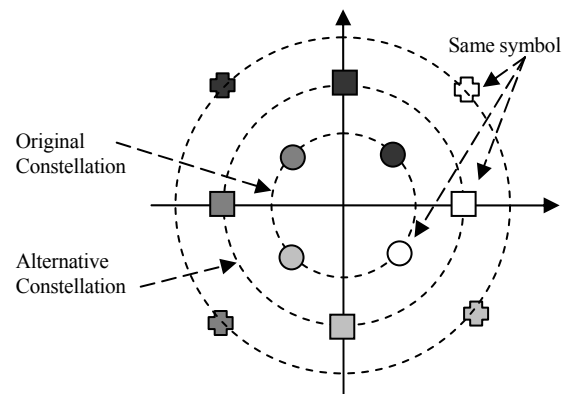


Figure 3. Expanded constellation for multiple symbol representations.

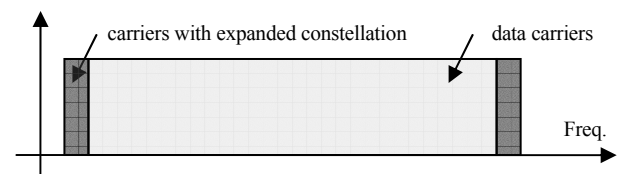


Figure 4. Usage of expanded constellation within an OFDM symbol.

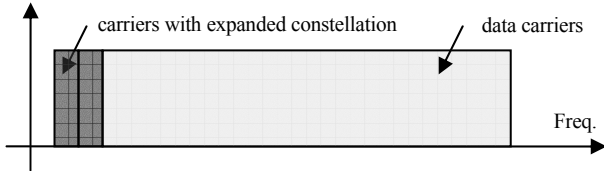


Figure 5. Usage of expanded constellation within an OFDM symbol.

To further reduce the PAPR a clipping technique [1] is applied next. It is presented in the block diagram from Fig.6 as well. Here the input vector  $[a_0, \dots, a_{N-1}]$  is first converted from frequency to time domain using an oversize IFFT. For the oversampling factor  $p$ , the input vector is padded with  $N(p-1)$  zeros placed in the middle of the vector. This results in a trigonometric interpolation of the time domain signal, which fits well for the signals with integral frequencies over the original FFT window, like is the case of OFDM. The interpolated signal is then clipped by limiting its amplitude. The clipping ratio is defined as the clipping level  $A$  divided by the root-mean-square power  $\sigma$  of the unclipped baseband signal.

$$CR = 20 \cdot \log_{10} \left( \frac{A}{\sigma} \right). \quad (4)$$

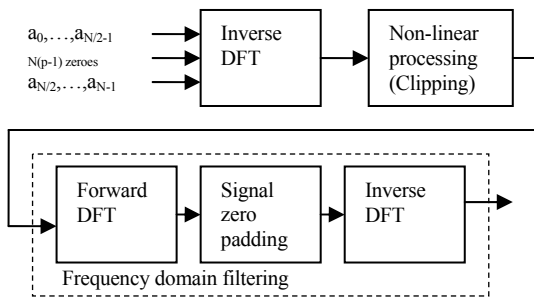


Figure 6. MATLAB model of the signal clipping based peak reduction technique.

In order to evaluate the performance of the proposed PAPR reduction scheme, the MATLAB simulator evaluates the complementary cumulative distribution function (CCDF) of the PAPR of the given OFDM signal. This is expressed as:

$$\begin{aligned} CCDF(Y) &= \Pr(PAPR > Y) = \\ &= 1 - \Pr(PAPR < Y) \end{aligned} \quad (5)$$

where  $Y$  is a PAPR threshold.

The literature provides a reference expression for CCDF of PAPR higher than the threshold  $r_0$  of OFDM with  $N$  subcarriers [14]:

$$CCDF(r_0) \approx 1 - \left(1 - e^{-r_0}\right)^N. \quad (6)$$

#### 4. NUMERICAL RESULTS

The MATLAB simulations have been performed for base-band OFDM symbols with different length and configurations, using M-QAM and M-PSK modulations with  $M=16$  and  $M=64$  constellation points.

The results presented in this paper are obtained for OFDM frames with the repartition of computing carriers as previously indicated in Fig.5. Within expanded constellation, the alternative points from each concentric circle have an offset of  $\varphi_e = \pi/4$  with their equivalents from the inner circle. The clipping rate defined in (4) has been set to a value of  $CR=12$ , and the filtering over-sampling factor was set to  $p=2$ .

The numerical results have shown that the new proposed scheme improves the PAPR reduction factor and the bit error rate (BER) in comparison with the simple signal clipping method used in its second step.

Fig.7 presents the CCDF of PAPR for a 16-PSK based OFDM signal with  $N=128$  carriers,  $Q=8$  selected carriers having  $R=9$  alternative points per symbol are used for peak reduction. The corresponding BER(SNR) characteristics, for a channel with Additive White Gaussian Noise (AWGN) in complex space, are presented in Fig.8.

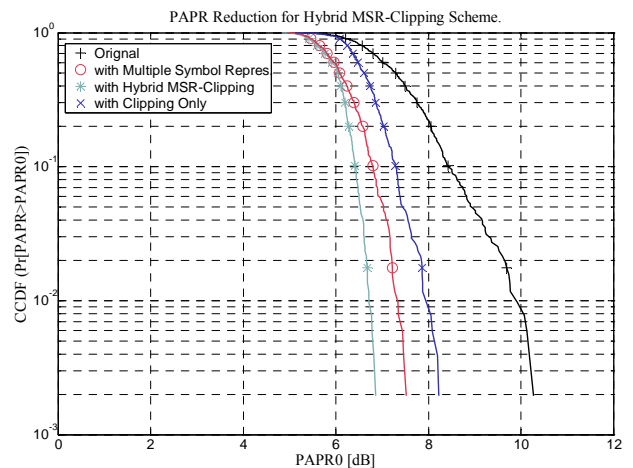


Figure 7. PAPR reduction of the OFDM signal.

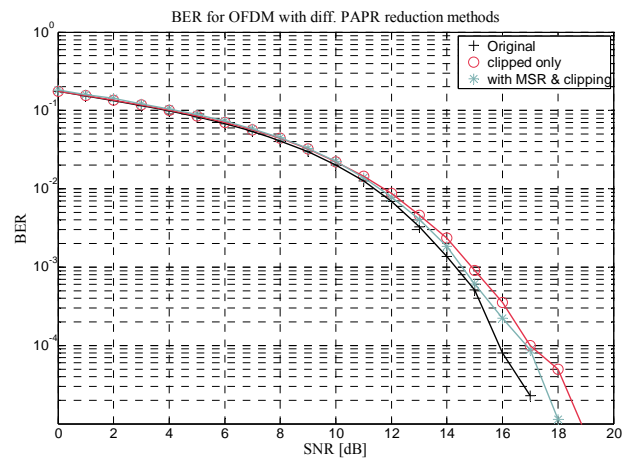


Figure 8. BER(SNR) for the OFDM signal when PAPR reduction methods are applied.

The results for the case when the phase offset is set to  $\varphi_e=0$  (alternative points being collinear) are presented in Fig. 9 and Fig. 10 respectively. The constant phase of the alternative symbols from this particular expanded constellation offers slight PAPR reduction, but a better BER performance. For the 16-QAM similar results have been obtained.

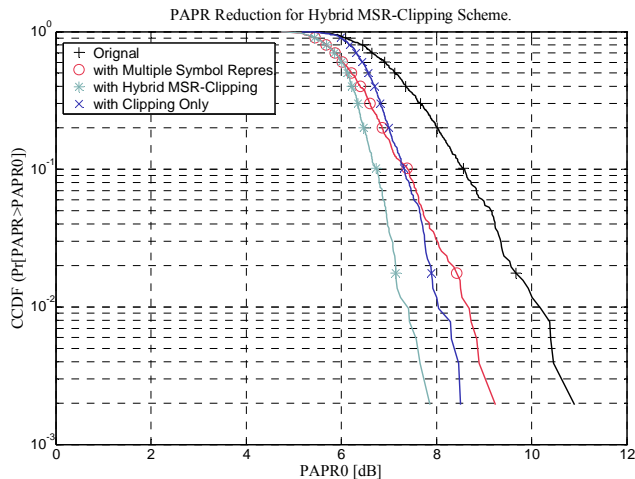


Figure 9. PAPR reduction of the OFDM signal.

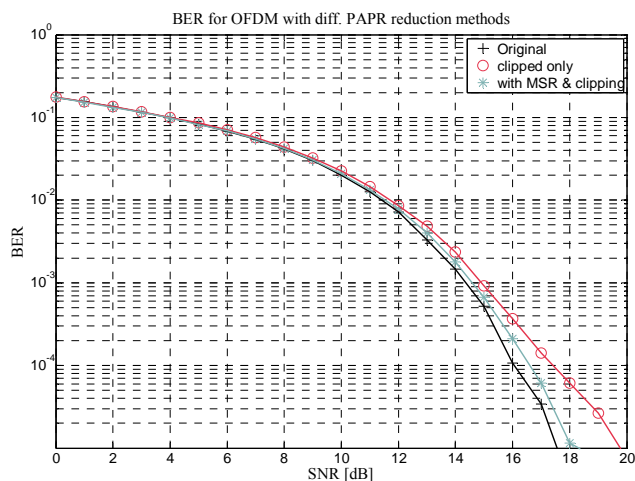


Figure 10. BER(SNR) for the OFDM signal when PAPR reduction methods are applied.

### 5. CONCLUSIONS

We presented a new hybrid PAPR reduction scheme. This technique is composed by a multiple symbol representations step followed by a signal clipping operation. This new PAPR reduction method combines the advantages of linearity from the first step with the reduced computation complexity of the second step, providing a better PAPR reduction with an insignificant bit error rate (BER) degradation.

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